

# Landmark transfer with Minimal Graph

★ submission to 3DOR

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15 Nov. 2012

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• IGG

★ Eurographics Workshop on 3D Object Retrieval

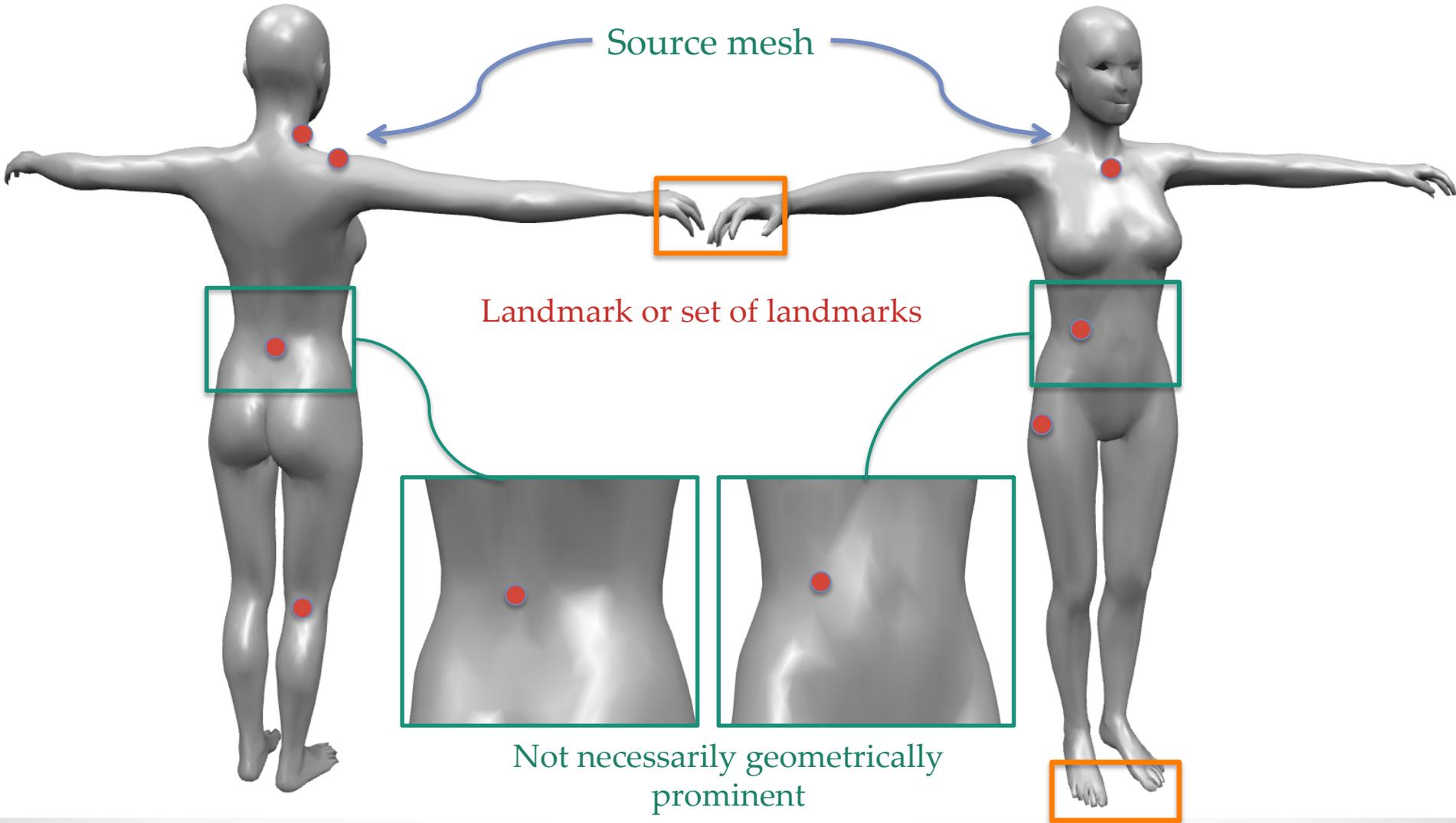


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# Overview

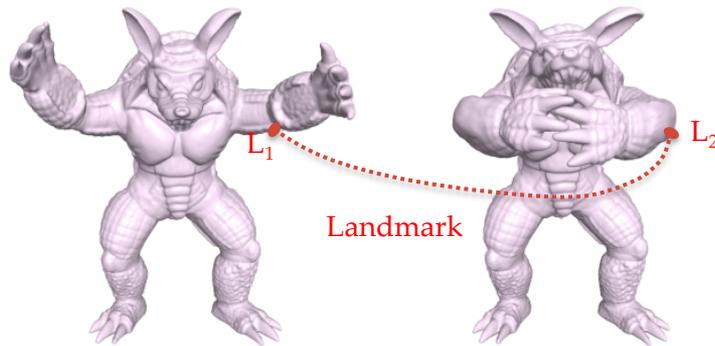
- Goal and Motivation
- Related approaches
- Landmark transfer technique
- Results
- Future plans

# What is landmark?

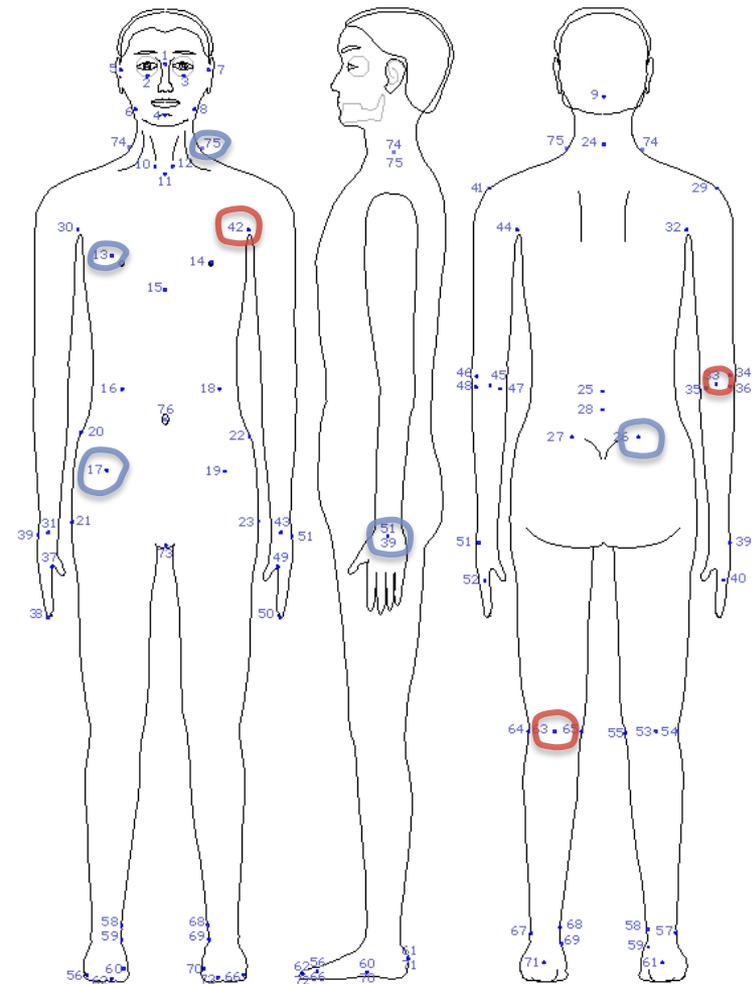


# Why landmarks?

- Correspondence computation
- Shape analysis
- Anthropometric studies
- Initial step in full shape registration
- Reuse of application-specific **landmarks**

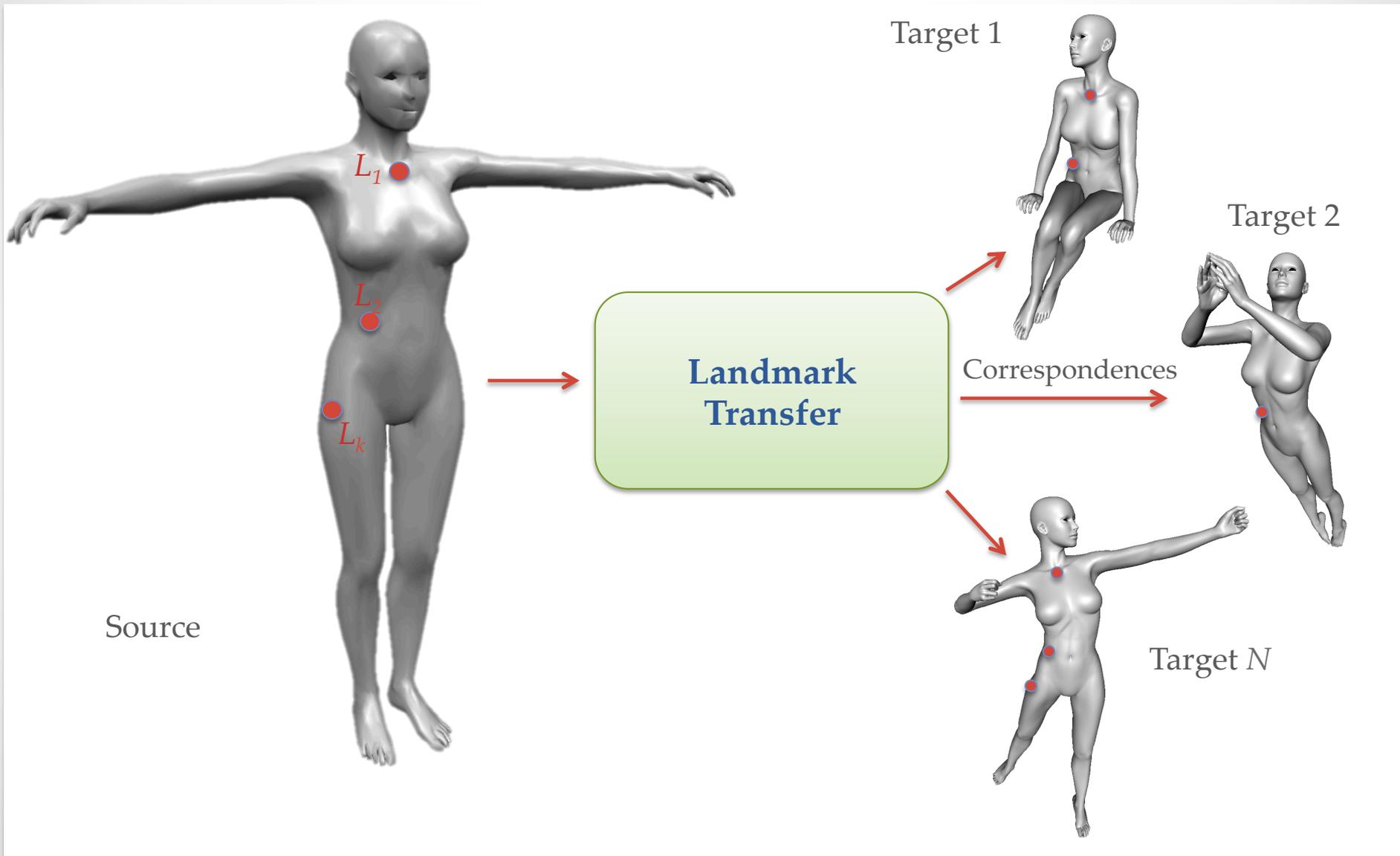


[The Armadillo AIM@SHAPE ]



[Feature points for the human body, Humanoid animation]

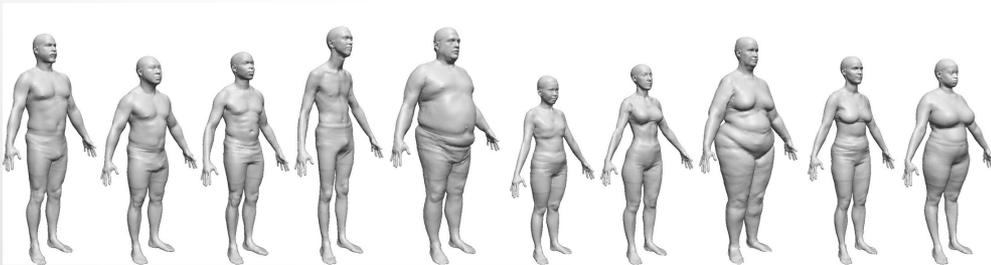
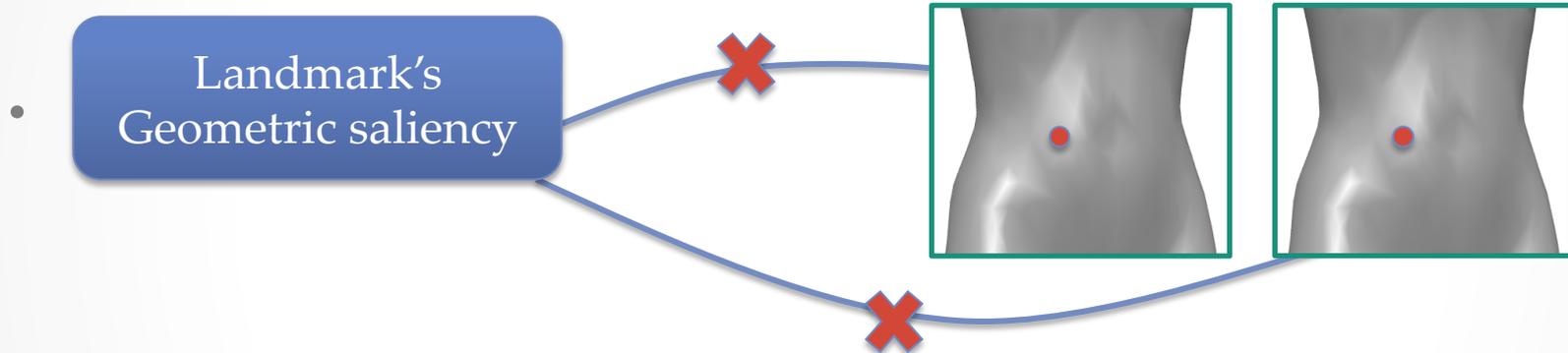
# Objective



# Objective

## Requirements:

- **Robust and fast**
- **Transferred landmarks** are **persistent** across pose change
- Transfer efficiently to collection of **multiple target shapes**

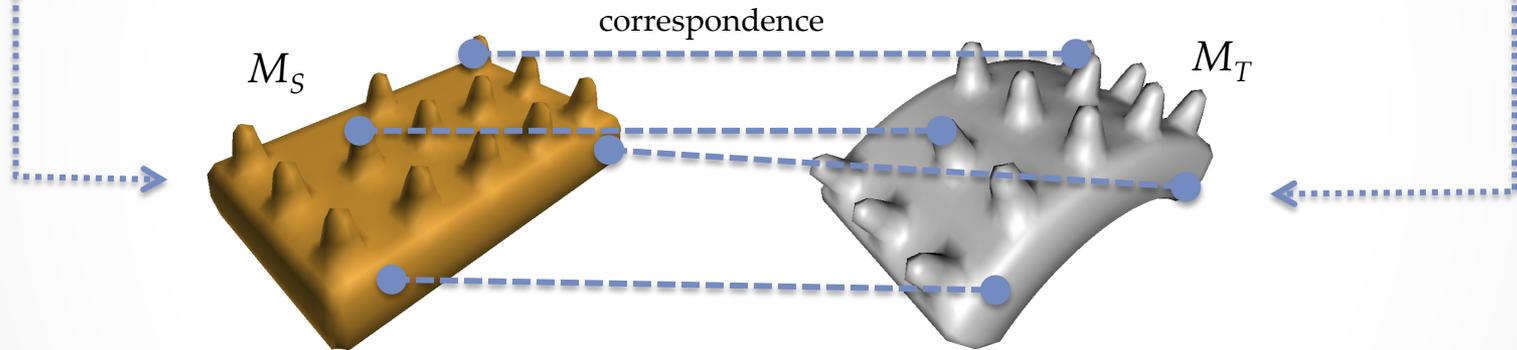


[CAESAR Project], etc.

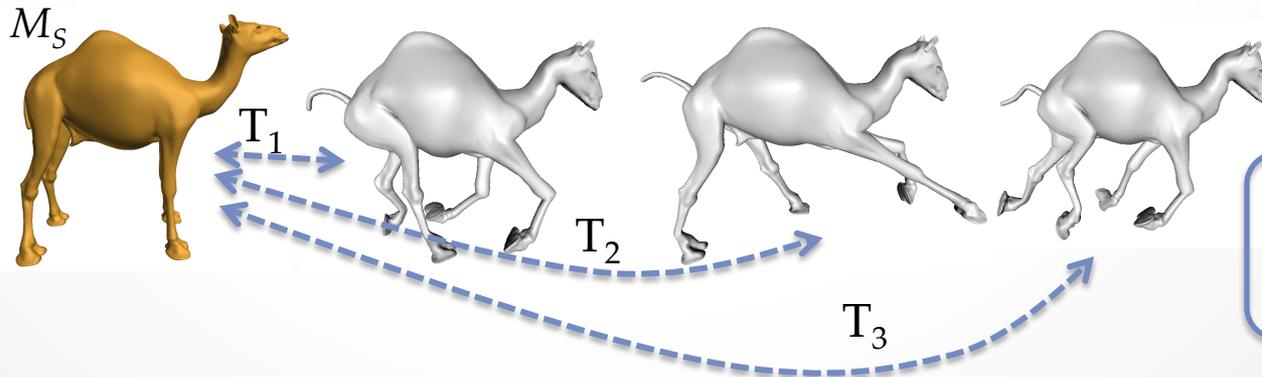
# Why interesting?

## Possible solution for landmark transfer:

- Approach as a problem of **full** shape registration
- Dense deformable shape registration gives us a set of all landmark correspondences



How about multiple targets?



Full registration is expensive

# Related approaches

- Goal and Motivation
- Related approaches
- Landmark transfer technique
- Results
- Future plan

# Related work

Nouvelle technique: there were no previous work on user-driven landmark transfer

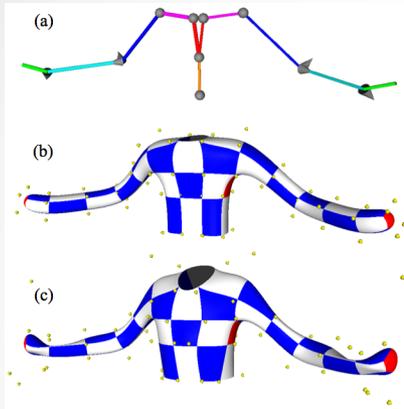
Relevant publications:

- [Allen et al.]'02
  - [Allen et al.]'03
  - [Seo et al.]'03
  - [Chang et al.]'08
  - [Huang et al.]'08
  - [Tevs et al.]'09
  - [Tevs et al.]'11
- manual
- regular
- planned
- 
- The diagram shows a list of seven publications. The first three are grouped under 'manual' with an orange bracket. The next three are grouped under 'regular' with a grey bracket. The last one is grouped under 'planned' with a black bracket. A large blue bracket on the right encompasses all seven publications, and an arrow points from this bracket to a text box on the right.

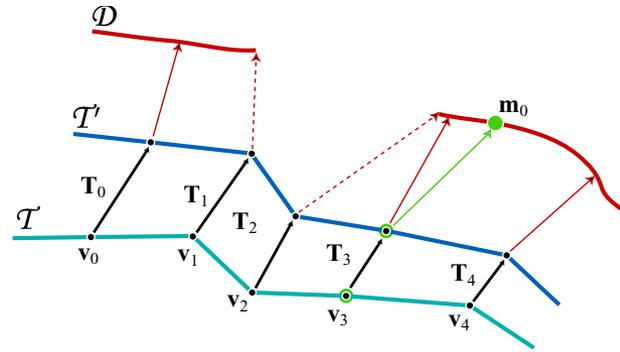
Registration techniques which rely on initial sparse and coherent correspondences

No shape is completely deformable. Every deformable shape matching method uses some deformable model

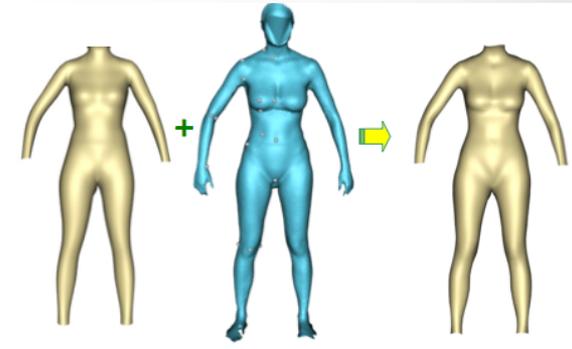
# Marker correspondence: manual



[Allen et al.]'02



[Allen et al.]'03



[SEO et al.]

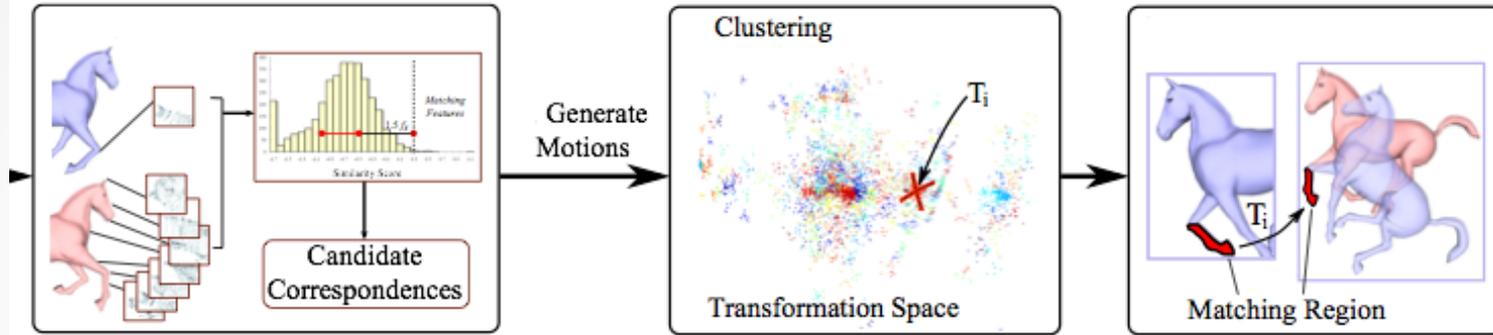
Manual marker assignment is used to drive ICP:

$$\operatorname{argmin}(\alpha \cdot E_{data} + \beta \cdot E_{smoth} + \gamma \cdot E_{marker})$$

- B. Allen, B. Curless, Z. Popović, The space of human body shapes: reconstruction and parameterization from range scans, Proc. ACM SIGGRAPH, pp.587-594, 2003.
- B. Allen, B. Curless, Z. Popović, Articulated body deformation from range scan data, SIGGRAPH 2002, July 2002, San Antonio, Texas.
- H. Seo, N. Magnenat-Thalmann, An automatic modeling of human bodies from sizing parameters, Proc. ACM symposium on Interactive 3D graphics, pp.19-26, 2003.

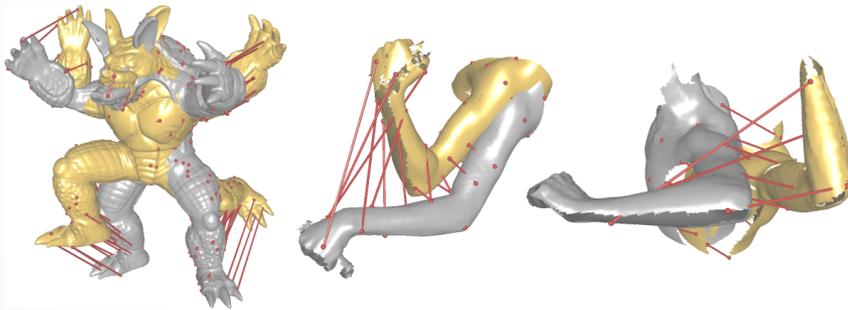
# Marker correspondence: regular

[Chang et al.]



Poisson sampling

[Huang et al.]



Octree sampling

Q.-X. Huang, B. Adams, M. Wicke, L. J. Guibas, Non-Rigid Registration Under Isometric Deformations, Proc. of the Symposium on Geometry Processing, pp.1449-1457, 2008.

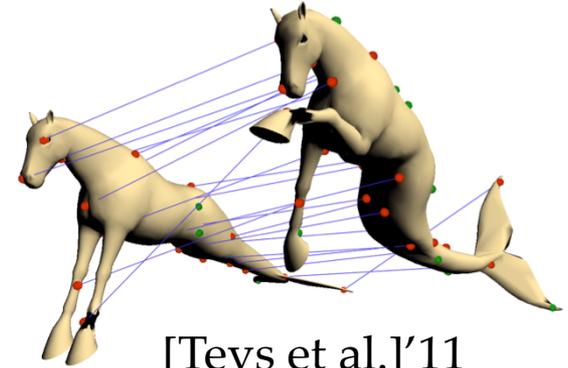
W. Chang, M. Zwicker, Automatic Registration for Articulated Shapes, Computer Graphics Forum (Proceedings of SGP 2008), 1459-1468, 2008.

# Marker correspondence: planned



[Tevs et al.]'09

- Random sampling



[Tevs et al.]'11

Planned sampling

A. Tevs, M. Bokeloh, M. Wand, A. Schilling, H.-P. Seidel, Isometric Registration of Ambiguous and Partial Data, Proc. IEEE Conference on Computer Vision and Pattern Recognition (CVPR '09), 2009.

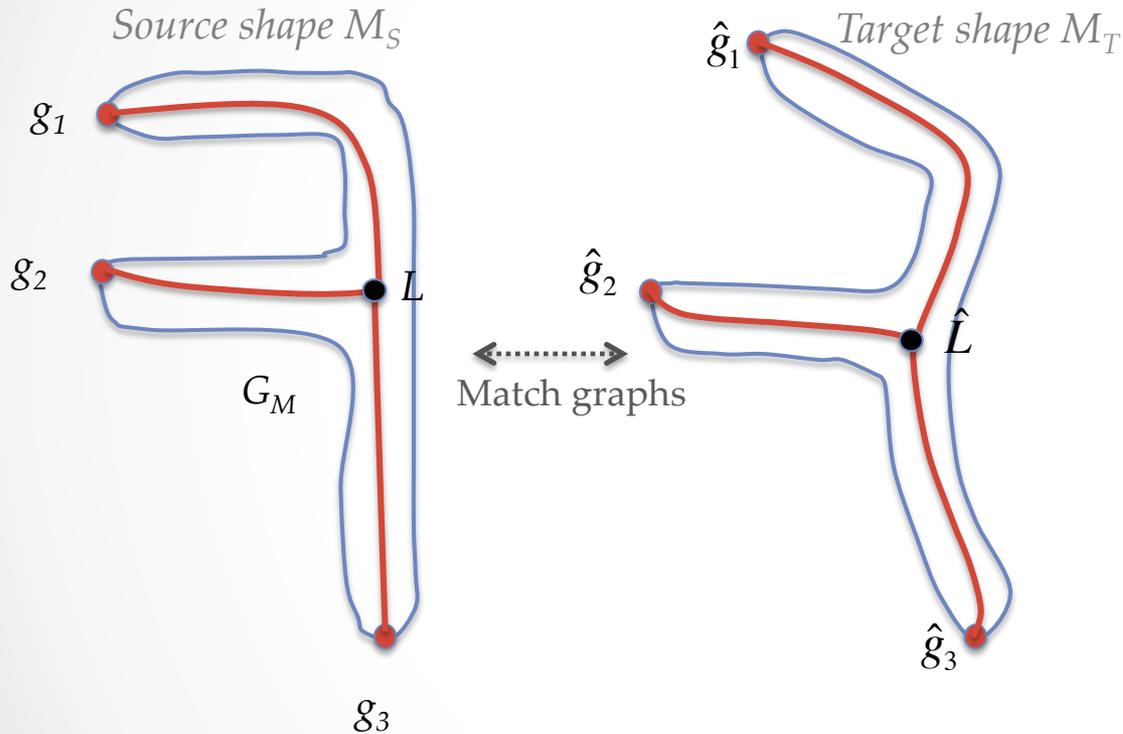
A. Tevs, A. Berner, M. Wand, I. Ihrke, H.-P. Seidel, Intrinsic Shape Matching by Planned Landmark Sampling", Eurographics, 2011

# Landmark Transfer

- Goal and Motivation
- Related approaches
- Landmark transfer technique
- Results
- Future plan

# Landmark transfer: key idea

**Assumption:** shapes are approximately **isometric**



Define landmark position  $L$  with respect to geometric features and **geodesic distances** to them



Graph  $G_M$

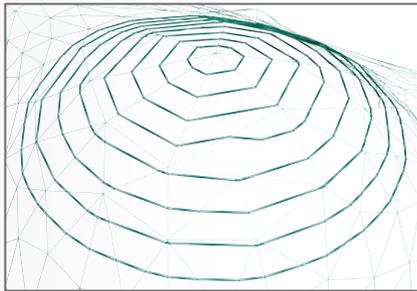
- Sufficient to define landmark
- As small as possible
- Unique

# Intrinsic wave descriptor

- In spirit of [Tevs et al.]
- **Isometry invariant**

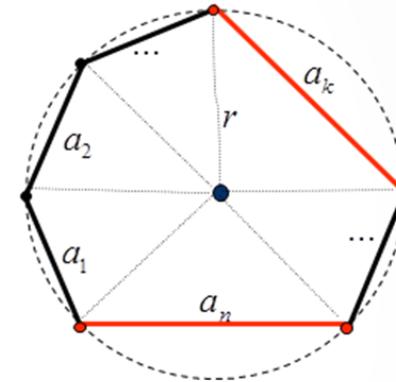
$$D_x = \left( \frac{l_1}{2\pi r_1}, \frac{l_2}{2\pi r_2}, \dots, \frac{l_{16}}{2\pi r_{16}} \right)^T$$

Intrinsic wave descriptor  
polygonal approximation



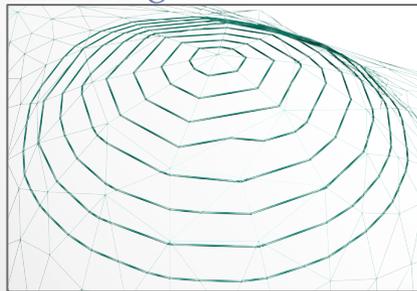
$$\exists a \in l_i : a \geq 0.1p(l_i)$$

Problem

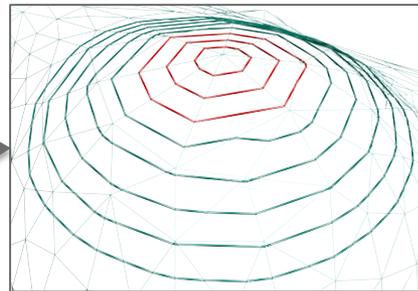


Further we **modify** IWD towards robustness to mesh sampling:

Original IWD



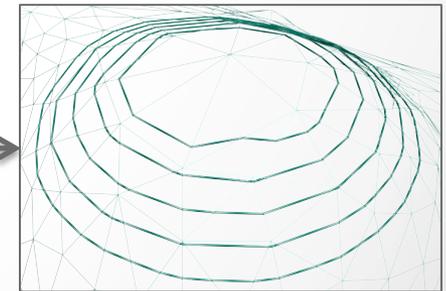
Firstly



Identify distorted  
iso-contours

Secondly

Modified IWD



Retain  $[\mu + \sigma]$

• IGG  
All iso-contours

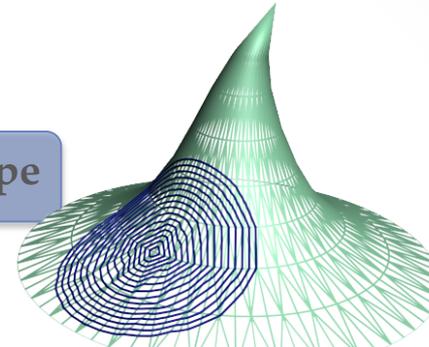
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# Extracting extremities

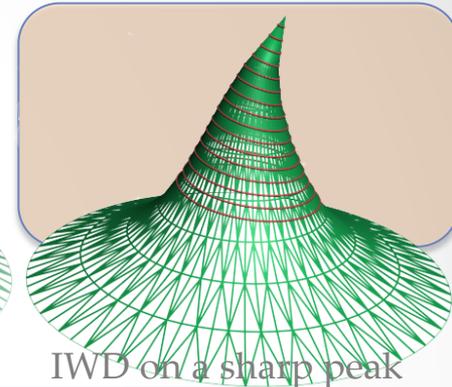
**Def.** Given modified intrinsic wave descriptor,  $D'_x$

$$\gamma(x) \equiv \left\| D'_x \right\|_2^{-1}$$

- Increases on the “sharp” features of the shape
- Comes up to  $+\infty$  for a vertex on the tip of an infinitely sharp, needle-like shape

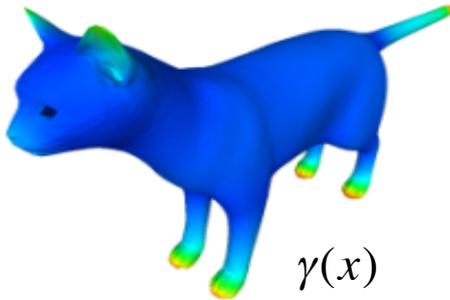


IWD on a flat patch



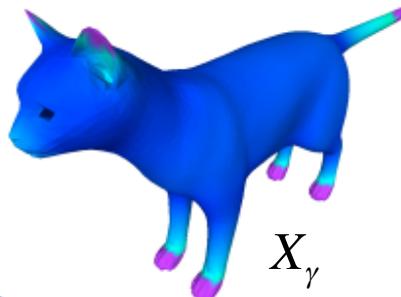
IWD on a sharp peak

Compute convexity  
over the mesh



Step 1

Retain most prominent set  
with respect to  $\gamma(x)$



Step 2

Cluster  $X_\gamma$  and extract  
extremities

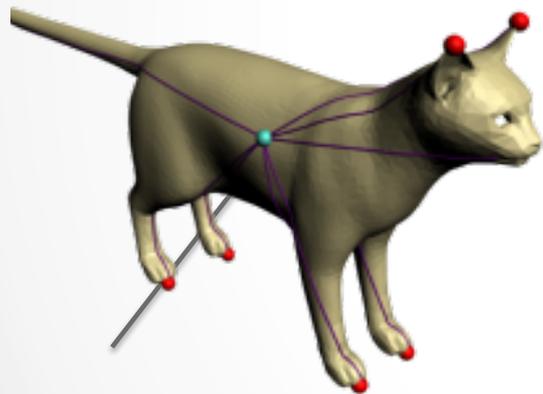
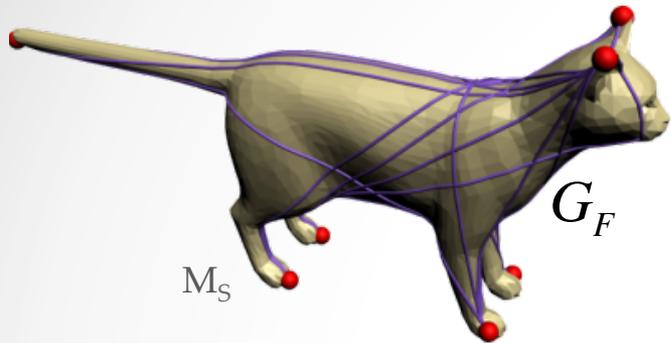


Step 3

$$\arg \max_{x \in C_{\gamma,i}} \delta(g, x)$$

# Landmark Transfer

Convexity extremities  $\rightarrow$  full graph  $G_F$



Compute a minimal graph for user-provided landmark

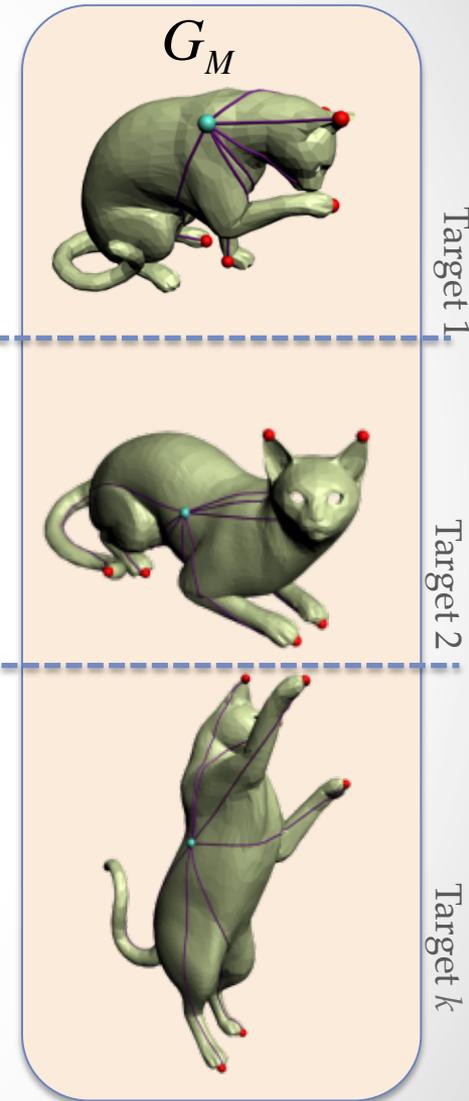
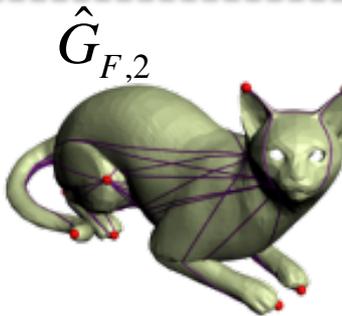
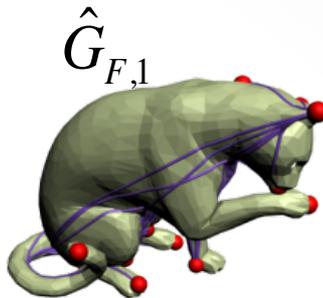
$G_M$

Graph Matching [Ullmann]

Matching 1

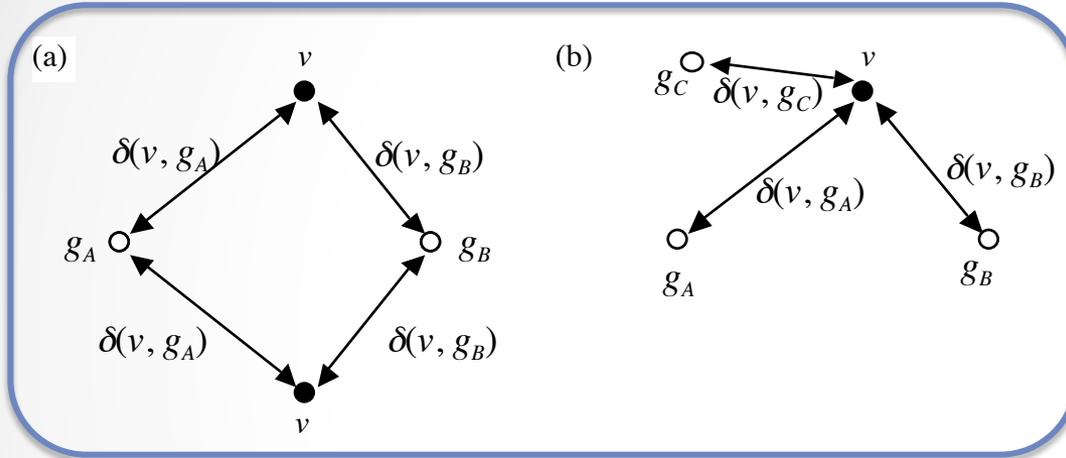
Matching 2

Matching  $k$



# Minimal graph $G_M$ construction

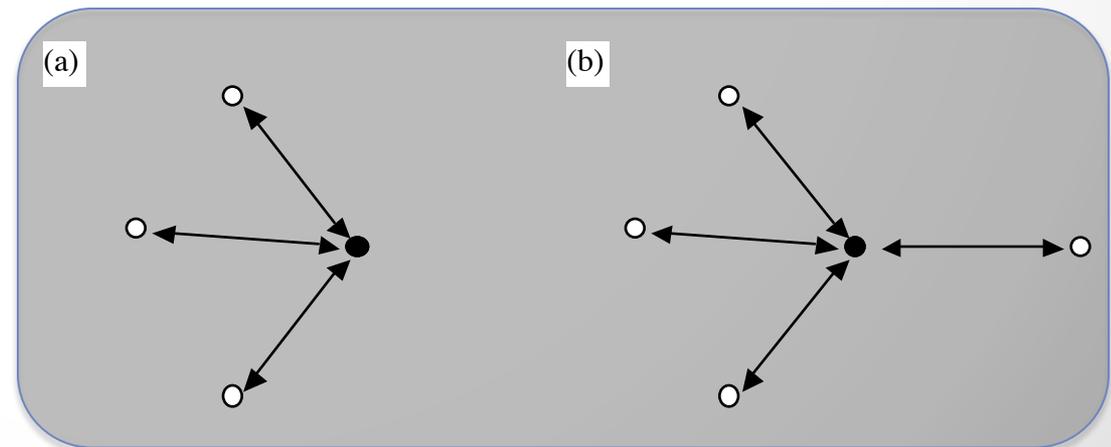
1. Position of the landmark is uniquely defined by its geodesic distances to each node in the minimal graph



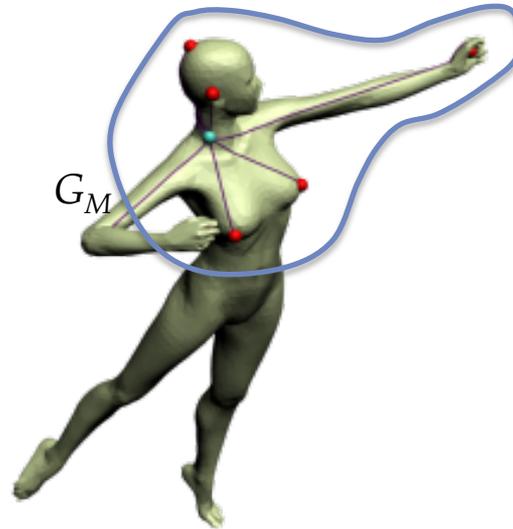
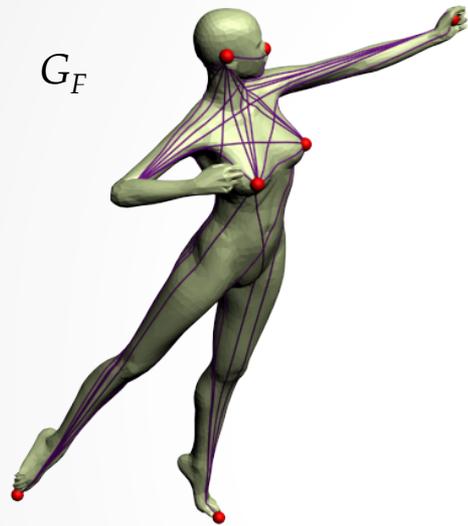
2. The landmark is inside a convex hull of the N-gon formed by the graph nodes

3. The minimal graph is a unique subgraph of the full graph

Checked by self-matching on the shape via Ulmann's approach



# Minimal graph



Compact graph  
is preferred



Less desirable

# Landmark transfer

$M_S$  – source shape,  $M_T$  – target shape

$$G_M = \{V_M, E_M\}$$

**Feature point coordinates** (*FP-coordinates*) of  $v$ :

$$\delta_{M_S}(v) = (\delta(v, g_1), \dots, \delta(v, g_k))^T$$

// FP-coordinates on the source  $M_S$

Transferred point  $\hat{v}$  must satisfy:

$$\delta_{M_T}(\hat{v}) = \delta_{M_S}(v)$$

$$\delta_{M_T}(\hat{v}) = (\delta(\hat{v}, \hat{g}_1), \dots, \delta(\hat{v}, \hat{g}_k))^T$$

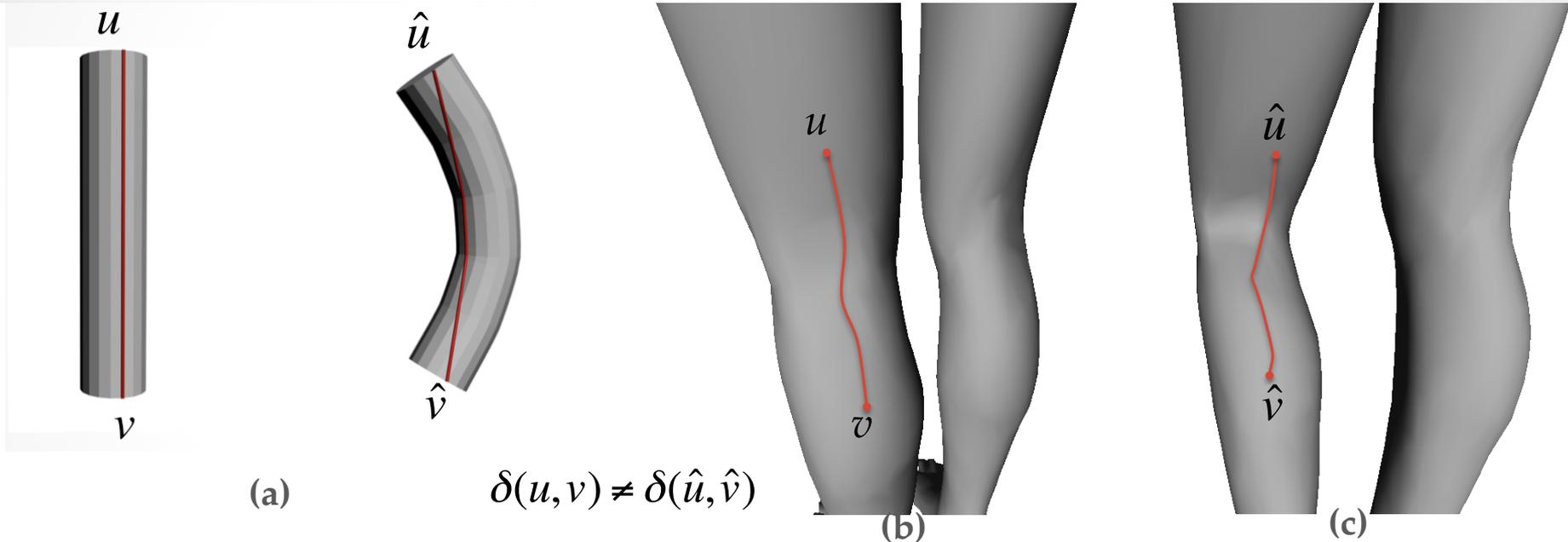
// FP-coordinates on the target  $M_T$

However, in practice:

$$\delta_{M_T}(\hat{v}) \neq \delta_{M_S}(v)$$

# Geodesic distance changes

Geodesic distance as a shortest distance on the surface:



## Problem:

- Geodesic path and its length changes between  $u$  and  $v$  with a mesh deformation (a) (b) (c)
- In our experiments we observed up to 9% of change in geodesic distances

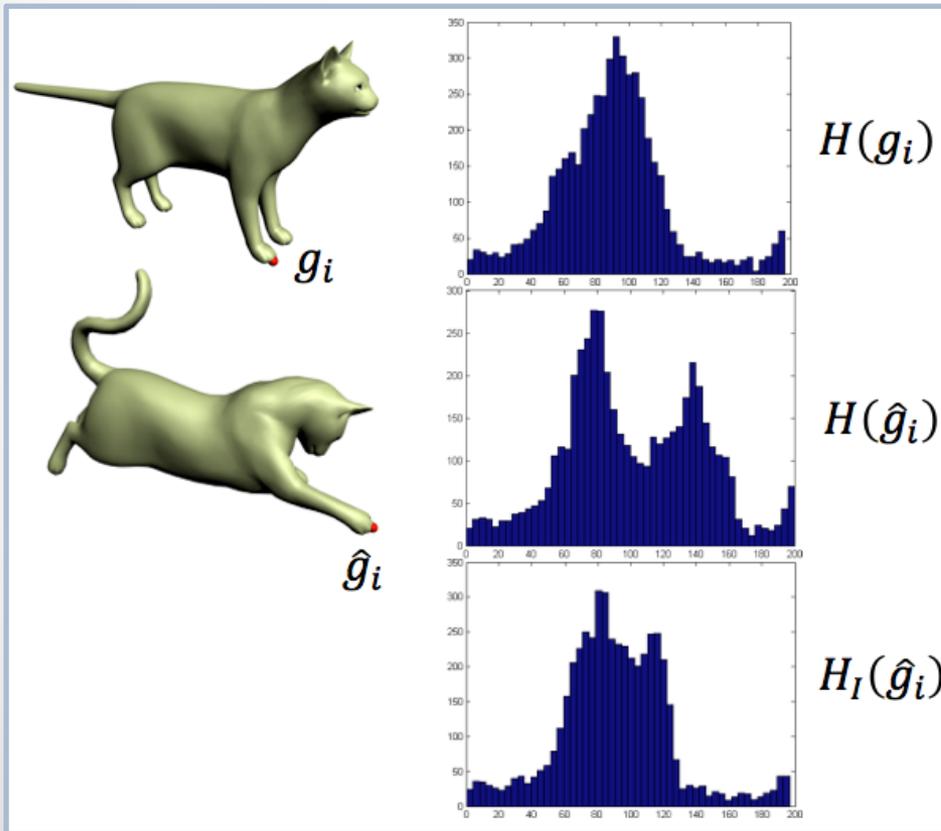
## Solution:

- Modify geodesic distances on the target to make them similar to those on the source

# Landmark transfer

$H(g_i)$  - geodesic distance histogram

Def. Distribution of the geodesic distances between the vertex  $g_i$  and all other vertices of the mesh  $M_S$



Histograms  $H(g_i)$  and  $H(\hat{g}_i)$  might be dissimilar for corresponding vertices

Interpolated geodesic histograms make values of geodesic distances on the target closer to the source

# Interpolating geodesic distances

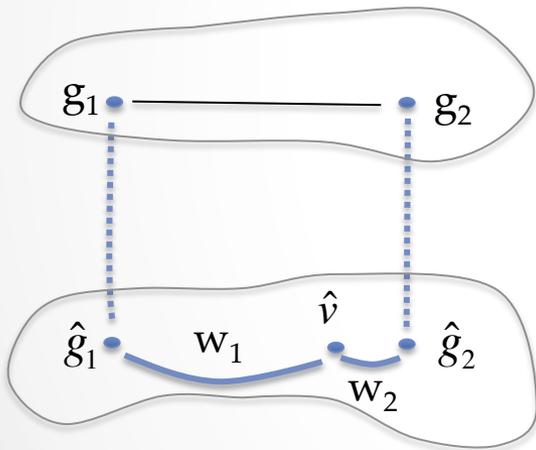
**Def.**  $\delta_I(\hat{v}, \hat{g}_i)$  interpolated geodesic distance:

$$\delta_I(\hat{v}, \hat{g}_i) = \sum_{j=1}^{\hat{n}_M} \frac{w_j(\hat{v}) \cdot \delta(g_j, g_i)}{\sum_{k=1}^{\hat{n}_M} w_k(\hat{v})}, \quad \text{where } w_j(\hat{v}) = \frac{1}{\delta(\hat{v}, \hat{g}_j)^{p_j}}$$

Inverse distance weighting

Get power parameters  $p_j$  solving  $\operatorname{argmin}_{p_j} (d(H_I(\hat{g}_i), H(g_i)))$

$d$  is a histogram metric [Earth Mover's Distance]



RUBNER Y., TOMASI C., GUIBAS L. J.: The earth mover's distance as a metric for image retrieval. *Int. J. Comput. Vision* 40, 2 (2000), 99–121.

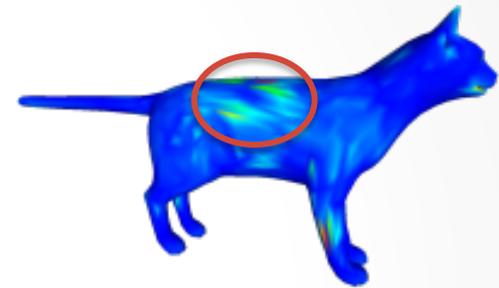
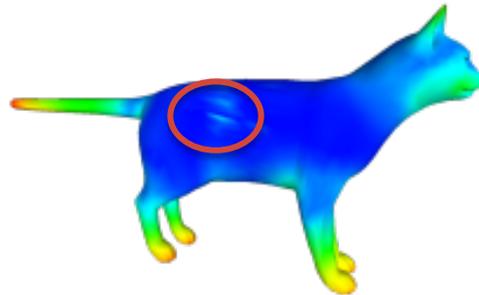
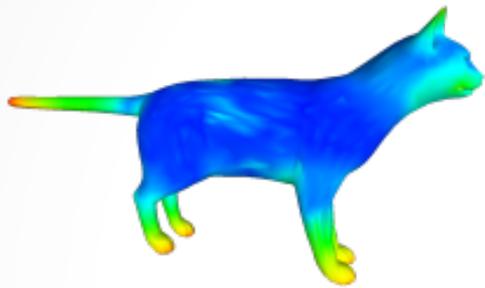
# Results

- Goal and Motivation
- Related approaches
- Landmark transfer technique
- Results
- Future plan

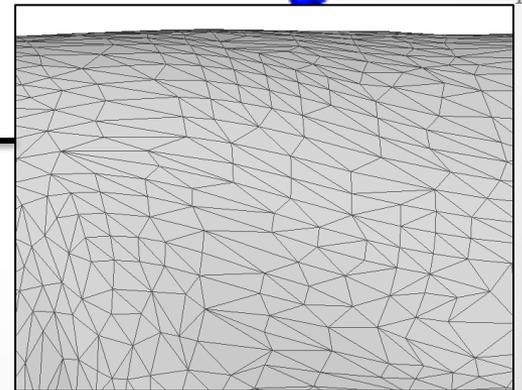
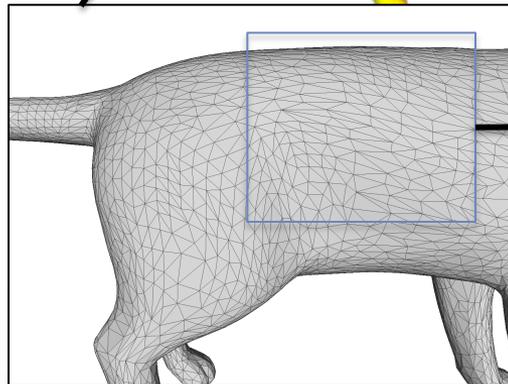
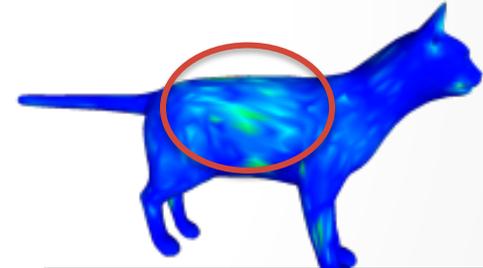
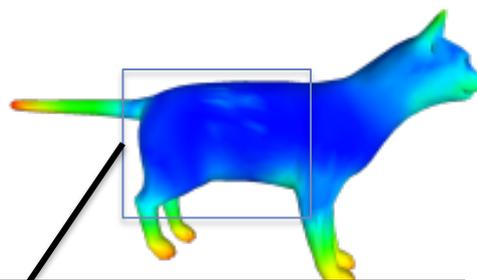
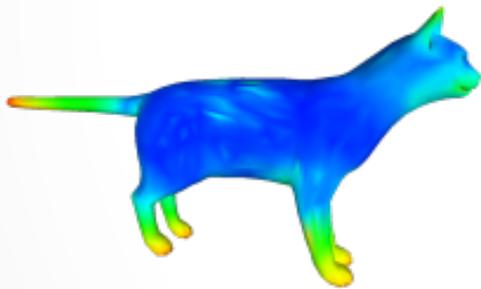
# Evaluation of the modified wave descriptor

Original IWD      Modified IWD      Difference map

Original mesh (5K)



Simplified mesh (2K)



# Results

Computational time:

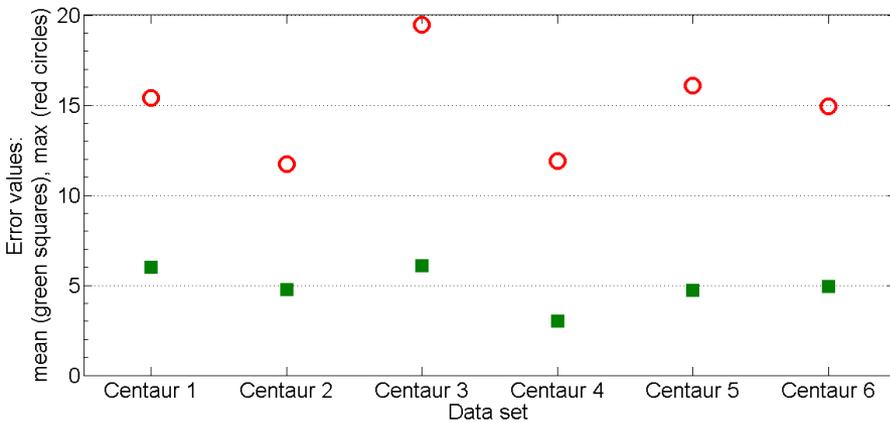
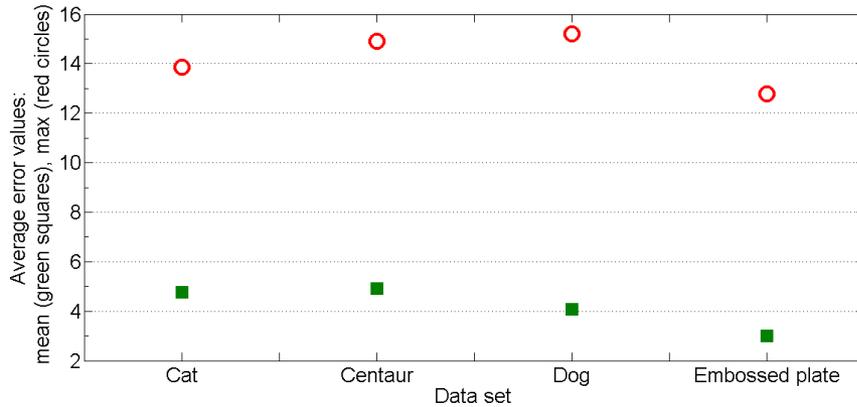
Data set	$ X $	$ T $	$ t_\delta $	$ t_{V_F} $	$ G_M $	$ t_{\hat{V}_F}  +  t_{\hat{G}_M} $	$ t_H $
Cat	4994	9977	146ms	21ms	39ms	59ms	6.63s
Centaur	5002	10000	86ms	23ms	128ms	338ms	48.96s
Dog	5000	9991	104ms	20ms	33ms	39ms	5.98s
Embossed plate	1482	2960	19ms	7ms	85ms	1708ms	2.81s

10 cat models, 5 centaur models, 7 dog models from TOSCA Shape Repository  
3 synthetic embossed plates

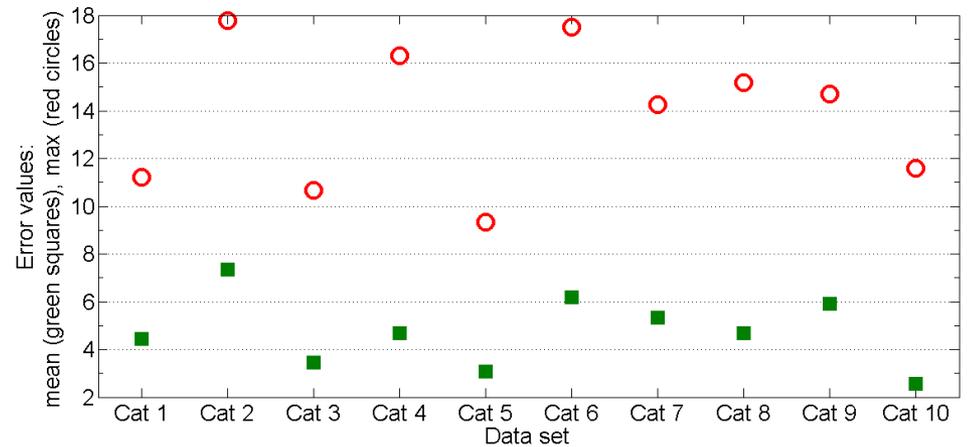
- Matlab implementation
- Update of geodesic distances is the most time consuming task
- Update of geodesics according to the histograms is required to be computed only once per each target mesh

# Results

Quality of transfer (QoT) with respect to ground truth



- Mixed data set of different subjects in different postures

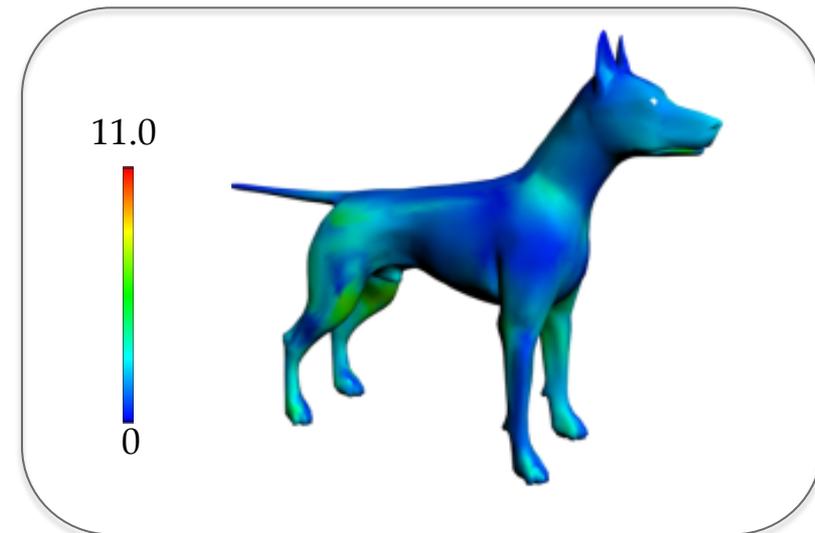
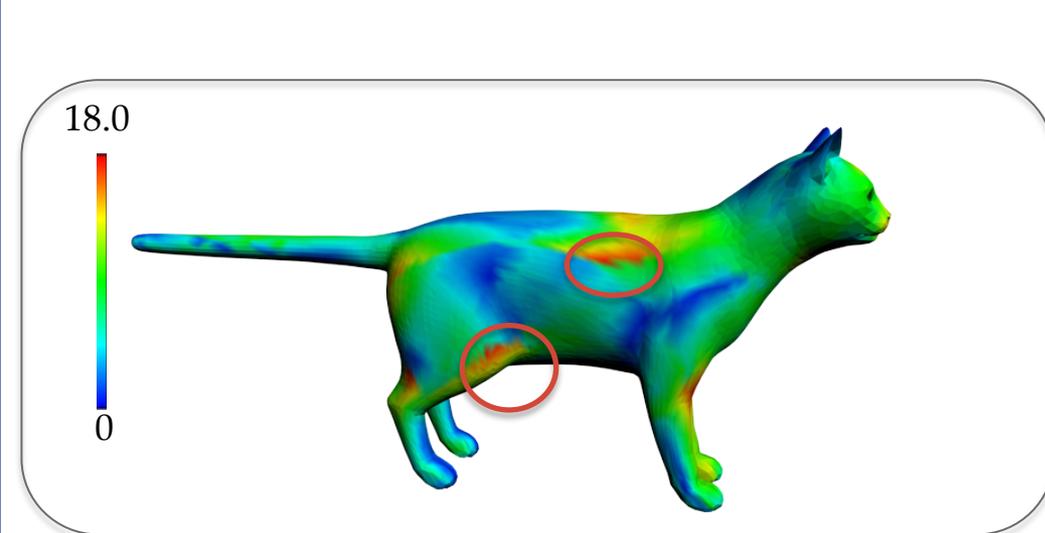
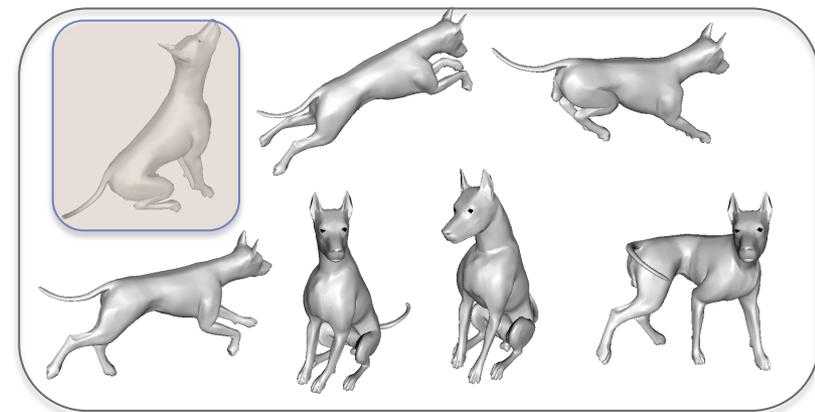
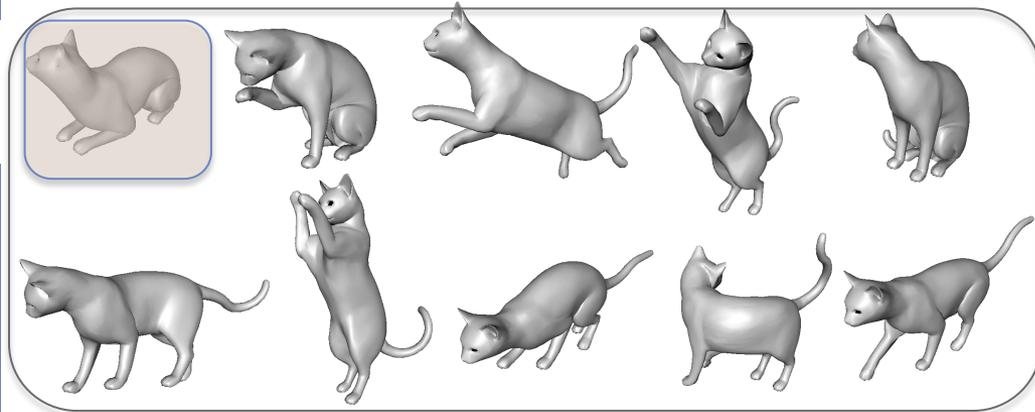


- Mean and Max error values vary from one posture to another due to imperfect isometries

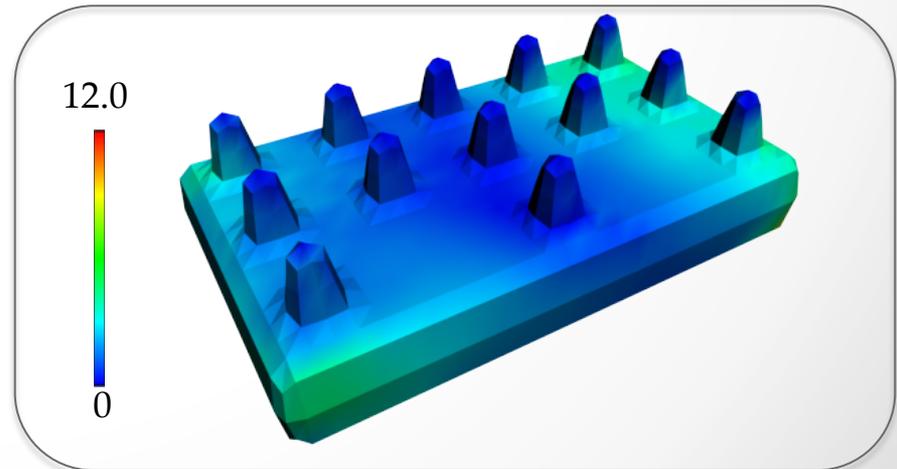
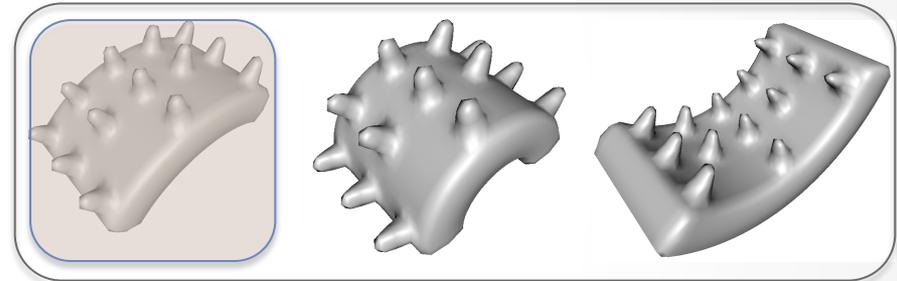
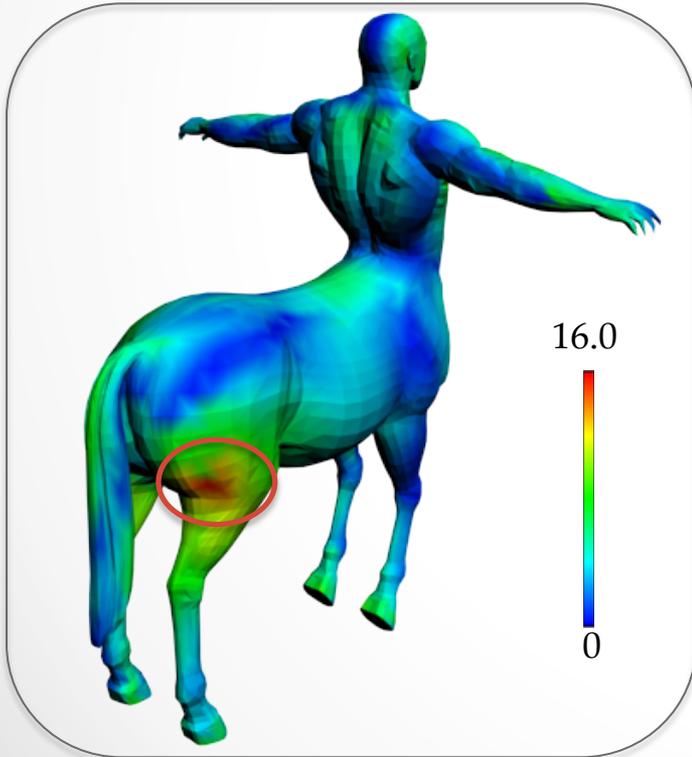
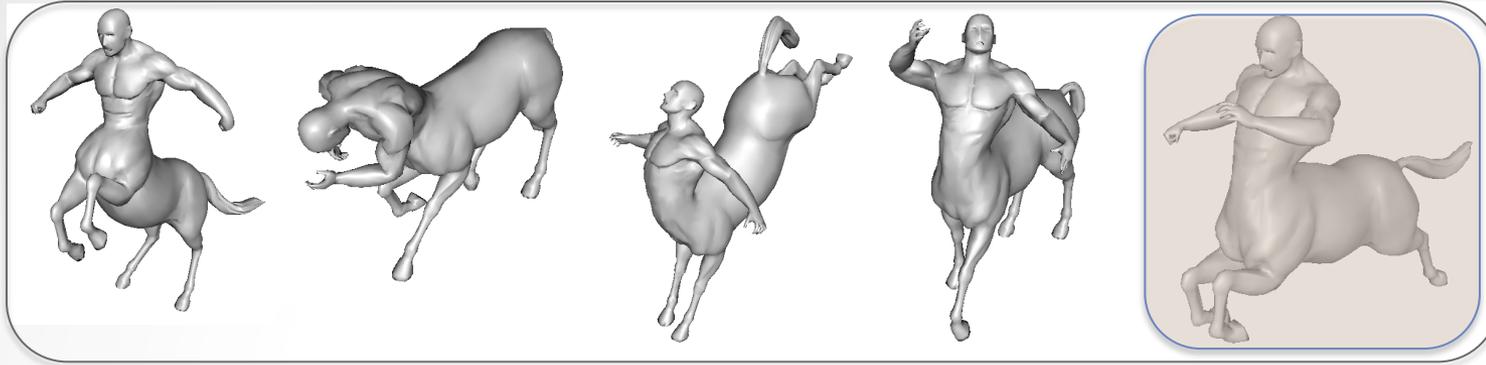
○ max error  
■ mean error

# Results

Quality of transferred landmark: the QoT is compared with the ground-truth correspondences from high-resolution TOSCA models

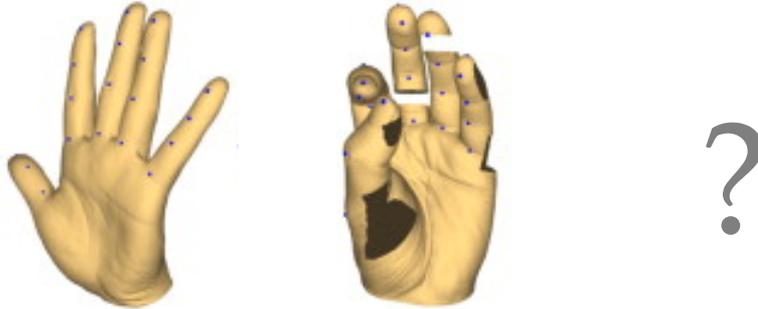


# Results

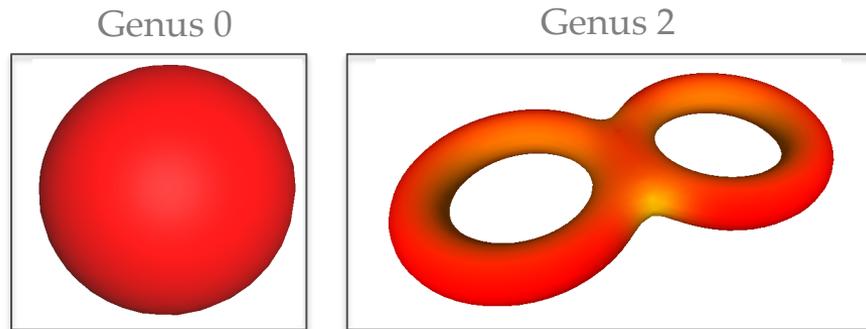


# Limitations

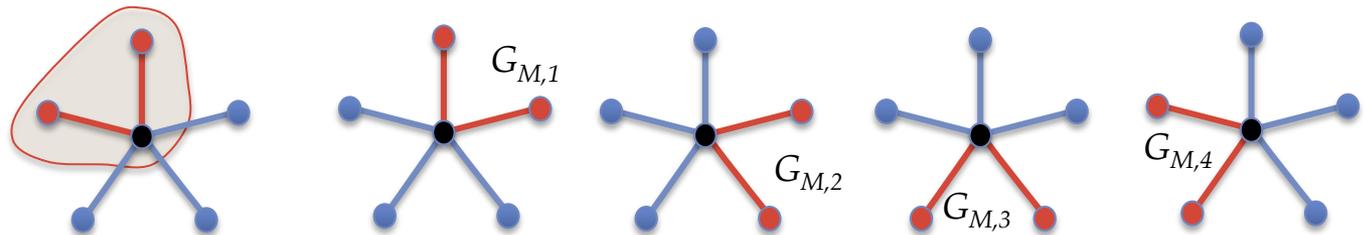
- Missing data? Holes?



- Featureless objects



- Symmetry



Problem of intrinsic symmetries

# Future plans

- Extension to full matching
- Maximum reuse of  $G_M$  for the correspondence computation

- Dynamic mesh registration 4D (3D +  $t$ )
- geometric + dynamic features
- Registration speed up by using Spatial segmentation -> registration of segments

# Acknowledgements

For assistance in comparison of Plansac method to our landmark transfer technique, we would like to thank Art Tevs and the authors of Plansac paper [TBW\*11] Alexander Berner, Michael Wand, Ivo Ihrke, and Hans-Peter Seidel.

Would like to thank Frederic Cordier for assistance in implementation.

**This work has been supported by the French national project SHARED (Shape Analysis and Registration of People Using Dynamic Data, No.10-CHEX-014-01).**

## References

- [BMS\*11] P. Bosea, A. Maheshwaria, C. Shub, S. Wuhrer, A survey of geodesic paths on 3D surfaces, *Computational Geometry - Theory and Applications*, Volume 44, Issue 9, Pages 486–498, November 2011.
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